

Dalitz analysis of $D^0 \rightarrow K^- \pi^+ \eta$ decays at Belle

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We present the results of the first Dalitz plot analysis of the decay $D^0 \rightarrow K^- \pi^+ \eta$. The analysis is performed on a data set corresponding to an integrated luminosity of 953 fb^{-1} collected by the Belle detector at the asymmetric-energy e^+e^- KEKB collider. The Dalitz plot is well described by a combination of the six resonant decay channels $\bar{K}^*(892)^0 \eta$, $K^- a_0(980)^+$, $K^- a_2(1320)^+$, $\bar{K}^*(1410)^0 \eta$, $K^*(1680)^- \pi^+$ and $K_2^*(1980)^- \pi^+$, together with $K\pi$ and $K\eta$ S-wave components. The decays $K^*(1680)^- \rightarrow K^- \eta$ and $K_2^*(1980)^- \rightarrow K^- \eta$ are observed for the first time. We measure ratio of the branching fractions, $\frac{\mathcal{B}(D^0 \rightarrow K^- \pi^+ \eta)}{\mathcal{B}(D^0 \rightarrow K^- \pi^+)} = 0.500 \pm 0.002(\text{stat}) \pm 0.020(\text{syst}) \pm 0.003(\mathcal{B}_{\text{PDG}})$. Using the Dalitz fit result, the ratio $\frac{\mathcal{B}(K^*(1680)^- \rightarrow K^- \eta)}{\mathcal{B}(K^*(1680)^- \rightarrow K^- \pi^+)}$ is measured to be $0.11 \pm 0.02(\text{stat})_{-0.04}^{+0.06}(\text{syst}) \pm 0.04(\mathcal{B}_{\text{PDG}})$; this is much lower than the theoretical expectations (≈ 1) made under the assumption that $K^*(1680)$ is a pure 1^3D_1 state. The product branching fraction $\mathcal{B}(D^0 \rightarrow [K_2^*(1980)^- \rightarrow K^- \eta] \pi^+) = (2.2_{-1.9}^{+1.7}) \times 10^{-4}$ is determined. In addition, the $\pi\eta'$ contribution to the $a_0(980)^\pm$ resonance shape is confirmed with 10.1σ statistical significance using the three-channel Flatté model. We also measure $\mathcal{B}(D^0 \rightarrow \bar{K}^*(892)^0 \eta) = (1.41_{-0.12}^{+0.13})\%$. This is consistent with, and more precise than, the current world average $(1.02 \pm 0.30)\%$, deviates with a significance of more than 3σ from the theoretical predictions of $(0.51\text{--}0.92)\%$.

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I. INTRODUCTION

The understanding of hadronic charmed-meson decays is theoretically challenging due to the significant nonperturbative contributions, and input from experimental measurements thus plays an important role [1–3]. We present a Dalitz plot (DP) analysis [4] to study the dynamics of three body decay $D^0 \rightarrow K^- \pi^+ \eta$. This decay is Cabibbo-favored (CF) and proceeds via the $c \rightarrow s\bar{u}\bar{d}$ transition. Because of isospin symmetry, intermediate states of this decay (e.g., excited kaon states decaying into $K\pi$ or $K\eta$), and a -family mesons decaying into $\pi\eta$, are similar to those in $D^0 \rightarrow K_S^0 \pi^0 \eta$. The DP analysis of the latter channel has previously been performed, and the intermediate channels $K_S^0 a_0(980)^0$ and $\bar{K}^*(892)^0 \eta$ [5] were found to be dominant, but additional components of a nonresonant amplitude, $K_0^*(1430)\eta$, $K_S^0 a_2(1320)$, $\kappa\eta$, and combinations of these processes, were found to contribute significantly. However, the statistical power of that sample was too limited for

precise measurements to be made. The $D^0 \rightarrow \bar{K}^{*0} \eta$ decay is sensitive to the W -exchange diagram, which is important for the theoretical understanding of charm decays. The theoretical predictions of the branching fraction of this mode vary in the range $(0.51\text{--}0.92)\%$ depending on the method [1–3]. This is consistent with, but smaller than, the current experimental result of $(1.02 \pm 0.30)\%$ [6] obtained in the $D^0 \rightarrow K_S^0 \pi^0 \eta$ final state [5]. A more precise measurement of this branching fraction from $D^0 \rightarrow K^- \pi^+ \eta$ decays would test the theoretical predictions. The $K_0^*(1430)^\pm \rightarrow K^\pm \eta$ decay was observed by the BABAR experiment [7] and is awaiting confirmation. Experimentally, the ratio of $K_0^*(1430)$ decaying into $K\eta$ and $K\pi$ is $0.09_{-0.04}^{+0.03}$ [6], which is consistent with the theoretical prediction of 0.05 [8] which was made with the assumption that it is a pure 1^3P_0 state.

Decays of some other excited kaons to $K\eta$, including $K^*(1410)$, $K^*(1680)$ and $K_2^*(1980)$, were predicted by Refs. [8,9] but have not yet been observed. These states may have some interesting properties; $K^*(1410)$ may not be a simple 2^3S_1 state, and $K^*(1410)$ and $K^*(1680)$ are predicted to be a mixture of the 2^3S_1 and 1^3D_1 states. Assuming $K^*(1410)$ and $K^*(1680)$ are pure 2^3S_1 and 1^3D_1 states, respectively, the relative branching ratio of $K^*(1680)$ to $K\eta$ and $K\pi$ should be close to one (1.18 in

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Ref. [8] and 0.93 in Ref. [9]) Experimentally, no branching ratio measurement for the former channel has previously been made.

The nature of the $a_0(980)$ is still not clear. Since it is a dominant intermediate resonance in $D^0 \rightarrow K^- \pi^+ \eta$, we can collect a large sample of $a_0(980)^+$ decays to study its character further, e.g., to confirm the $\pi\eta'$ contribution to the $a_0(980)$ line shape in a Flatté model as measured by BESIII [10]. Such a study can also help determine the $\pi\eta$ and $K\bar{K}$ contributions to $a_0(980)$ precisely and understand its quark component.

Wrong-sign (WS) decays play an important role in studies of D^0 - \bar{D}^0 mixing and CP violation such as the first observation of D^0 - \bar{D}^0 mixing [11]. One possible mode for this, $D^0 \rightarrow K^+ \pi^- \eta$, will be reconstructed at Belle II, which aims at a data set fifty times [12] larger than that currently available from Belle. A time-dependent Dalitz analysis of this mode can be used to measure charm-mixing parameters, and for such a measurement an amplitude analysis of the right-sign decay, $D^0 \rightarrow K^- \pi^+ \eta$, is needed to obtain the CF decay model.

This paper is organized as follows. Section II briefly describes the Belle detector and data samples, and Sec. III discusses event selection and parametrizations of signal and background and presents the measurement of the overall branching fraction. In Sec. IV, we report the results of the DP analysis. The evaluation of the systematic uncertainties are discussed in Sec. V. Further study and discussion of the Dalitz fit results are presented in Sec. VI. Finally, the conclusions are presented in Sec. VII.

II. BELLE DETECTOR AND DATASETS

We perform a first Dalitz analysis of the decays $D^0 \rightarrow K^- \pi^+ \eta$ [13] using 953 fb $^{-1}$ of data collected at or near the $\Upsilon(nS)$ resonances ($n = 1, 2, 3, 4, 5$), where 74% of the sample is taken at the $\Upsilon(4S)$ peak, with the Belle detector [14] operating at the KEKB asymmetric-energy e^+e^- collider [15]. The Belle detector is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector (SVD), a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter comprised of CsI(Tl) crystals located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside of the coil is instrumented to detect K_L^0 mesons and to identify muons. A detailed description of the Belle detector can be found elsewhere [14].

III. EVENT SELECTION AND YIELDS

The signal decay chain consists of $D^{*+} \rightarrow D^0 \pi_s^+$ with $D^0 \rightarrow K^- \pi^+ \eta$ and $\eta \rightarrow \gamma\gamma$; D^* mesons are produced in $e^+e^- \rightarrow c\bar{c}$ processes, and the charge of the slow pion π_s tags the flavor of the D^0 meson [16]. To ensure charged

tracks are well reconstructed, each is required to have at least two associated hits of the SVD in the beam and azimuthal directions, separately. The slow-pion candidates are required to have the signed distances from the pivotal point to the helix to be within ± 1.0 cm in the transverse plane and within ± 3.0 cm along the direction opposite to the positron beam. A charged track is identified as a kaon by requiring a ratio of particle identification likelihoods [17] $\mathcal{L}_K/(\mathcal{L}_K + \mathcal{L}_\pi) > 0.7$, which are constructed using CDC, TOF, and ACC information; otherwise the track is assumed to be a pion. This requirement has efficiencies of 85% and 98% and misidentification rates of 2% and 10% for kaons and pions, respectively. The photon candidates are reconstructed from ECL clusters unmatched to any charged track. The ratios of their energy deposits in a 3×3 array of CsI(Tl) crystals to that in a 5×5 array centered on the crystal with maximum deposited energy are required to be more than 0.8. The energies of photon candidates used to form η , E_γ , must exceed 60 or 120 MeV in the barrel or endcap region. The η candidates must have $\gamma\gamma$ mass within ${}_{+0.05}^{-0.06}$ GeV/ c^2 of the nominal mass [6] which takes into account the asymmetric resolution, and to have momentum in the laboratory frame, p_η , larger than 1 GeV/ c . Furthermore, we require $|\cos\theta_\eta| = \left| \frac{E_{\gamma 1} - E_{\gamma 2}}{E_{\gamma 1} + E_{\gamma 2}} \right| \cdot \frac{E_\eta}{p_\eta}$ to be less than 0.8, which is optimized to suppress combinatorial background. A large set of simulated signal Monte Carlo (MC) samples, more than 25 million events, is produced to study the efficiency. These are generated uniformly in phase space with the EVTGEN [18] and JETSET [19] software packages, and the detector response is modeled by the GEANT3 [20]. The final-state radiation effect is taken into account using the PHOTOS [21] package.

Kaon and pion tracks with opposite charge are required to form a common vertex (the D^0 decay position) with fit quality χ_v^2 . The η candidates are mass-constrained assuming that they are produced at this decay vertex, and the resultant η momentum is added to the $K\pi$ system to obtain the D^0 momentum. The invariant mass of $K\pi\eta$, M , is required to satisfy the condition $1.80 \text{ GeV}/c^2 < M < 1.92 \text{ GeV}/c^2$. Then, the D^0 production vertex is constrained to the e^+e^- interaction point, with fit quality χ_b^2 . The π_s track is refit to this D^0 production vertex, with a fit quality denoted χ_s^2 , to improve the resolution of the released energy in D^{*+} decay, $Q \equiv M_{K\pi\eta\pi_s} - M_{K\pi\eta} - m_{\pi_s}$. The value of Q is required to be less than 15 MeV/ c^2 to suppress further combinatorial background. The D^* momentum in the center-of-mass frame, $p^*(D^*)$, is required to be greater than 2.4, 2.5, or 3.1 GeV/ c for data below, on, or above $\Upsilon(4S)$ energy, to reduce high-multiplicity events and combinatorial background. A consequence of this requirement is that the D^0 candidates from B decays are removed. After applying all of these selection criteria, there are on average 1.3 signal decay candidates per event. A best-candidate selection (BCS) method is applied to multicandidate events,

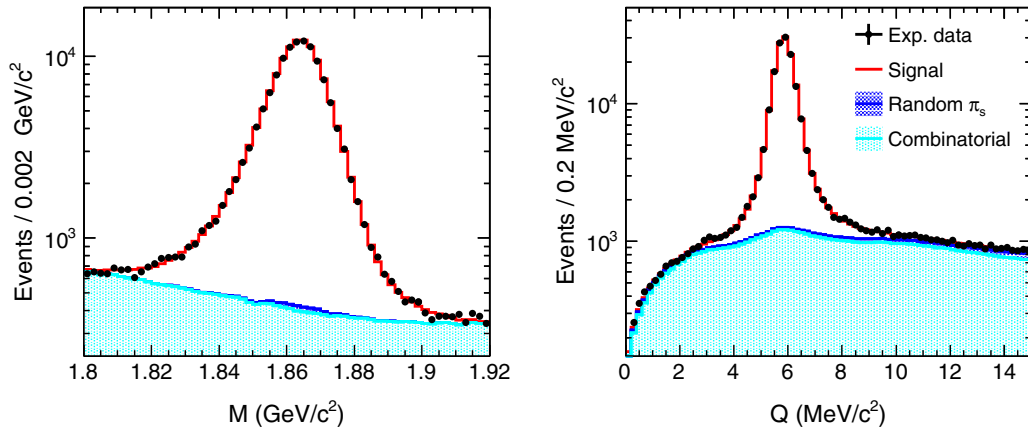


FIG. 1. The $D^0 \rightarrow K^- \pi^+ \eta$ reconstructed mass, M (in $5.35 \text{ GeV}/c^2 < Q < 6.35 \text{ GeV}/c^2$) and release energy of D^* decay, Q (in $1.85 \text{ GeV}/c^2 < M < 1.88 \text{ GeV}/c^2$) for experimental data (points with error bars) and fitted contributions of signal, random π_s and combinatorial backgrounds.

retaining as the best candidate the one with the smallest sum of vertex-fit qualities, $\chi_v^2 + \chi_b^2 + \chi_s^2$. A mass-constrained fit is then applied to the D^0 meson to improve resolution on the Dalitz variables, $M_{K\pi}^2$ and $M_{\pi\eta}^2$.

To extract yields of signal and background, a fit of the two-dimensional distribution of M and Q is performed. For the signal, the probability density function (PDF) in M is described by the sum of a double Gaussian and a double bifurcated Gaussian, with a common mean value (μ); the PDF in Q is described by the sum of a bifurcated Student function, a bifurcated Gaussian function, and a bifurcated Cruijff function [22], where the mean values and widths are correlated to the M value by a second-order polynomial function of $|M - \mu|$. For a real signal D^0 combined with a random π_s (named the random π_s background), the M distribution uses the same PDF as for the signal and the Q distribution uses a threshold function, $f(Q) = Q^\alpha e^{-\beta Q}$. This random background will be treated as signal, as it nearly consists of the same D^0 decay as the signal when the tiny fraction of DCS decay relative to CF decay is neglected. The combinatorial background is considered to have two components. A PDF smoothed by bilinear interpolation [23] is used for correlated combinatorial background, which has a correctly reconstructed π_s from D^* decay, but incorrectly reconstructed D^0 , whereas for other combinatorial background a third-order polynomial function of M and a threshold function of Q is used as a parameterization. The ratio between these two combinatorial backgrounds is fixed to that found using the generic MC. Figure 1 shows the M - Q combined fit for the experimental data. We obtain a signal yield of 105197 ± 990 in the M and Q two-dimensional (2D) signal region of $1.85 \text{ GeV}/c^2 < M < 1.88 \text{ GeV}/c^2$ and $5.35 \text{ MeV}/c^2 < Q < 6.35 \text{ MeV}/c^2$ with a high purity ($94.6 \pm 0.9\%$). These are the combinations that will be used for the fit to the Dalitz plot.

To measure the branching fraction of the decay $D^0 \rightarrow K^- \pi^+ \eta$, we normalize the signal yield by the number of D^0 mesons produced in the decay $D^{*+} \rightarrow D^0 \pi^+$. For normalization, we choose the $D^0 \rightarrow K^- \pi^+$ channel, which has a well-known rate of $\mathcal{B} = (3.950 \pm 0.031)\%$ [6]. We use the same selection criteria as are used $D^0 \rightarrow K^- \pi^+ \eta$ but without the η . We extract the signal yield from the distribution of D^0 invariant mass in $1.78 \text{ GeV}/c^2 < M < 1.94 \text{ GeV}/c^2$ and Q wide signal region $|Q - 5.85| < 1.0 \text{ MeV}/c^2$ and find signal yields of 116302 ± 510 for $D^0 \rightarrow K^- \pi^+ \eta$, and 2597343 ± 1669 for $D^0 \rightarrow K^- \pi^+$ (with a high purity 98.3%) based on the $\Upsilon(4S)$ on-resonance data set. The efficiency $\epsilon(D^0 \rightarrow K^- \pi^+ \eta) = (5.34 \pm 0.01)\%$ and $\epsilon(D^0 \rightarrow K^- \pi^+) = (23.49 \pm 0.02)\%$ are determined based on Dalitz signal MC produced with the nominal Dalitz fit result shown in Table I for $D^0 \rightarrow K^- \pi^+ \eta$ and signal MC for $D^0 \rightarrow K^- \pi^+$. Taking into account the branching fraction $\mathcal{B}(\eta \rightarrow \gamma\gamma) = (39.41 \pm 0.20)\%$ [6], we find the ratio of branching fractions to be

$$\frac{\mathcal{B}(D^0 \rightarrow K^- \pi^+ \eta)}{\mathcal{B}(D^0 \rightarrow K^- \pi^+)} = 0.500 \pm 0.002(\text{stat}) \pm 0.020(\text{syst}) \pm 0.003(\mathcal{B}_{\text{PDG}}), \quad (1)$$

where the three uncertainties shown are statistical, systematic, and the uncertainty of branching fraction of $\eta \rightarrow \gamma\gamma$, respectively. Using the known $D^0 \rightarrow K^- \pi^+$ branching fraction, we measure the branching fraction

$$\mathcal{B}(D^0 \rightarrow K^- \pi^+ \eta) = (1.973 \pm 0.009(\text{stat}) \pm 0.079(\text{syst}) \pm 0.018(\mathcal{B}_{\text{PDG}}))\%, \quad (2)$$

where the last error is associated with uncertainty of the branching fractions of $D^0 \rightarrow K^- \pi^+$ and $\eta \rightarrow \gamma\gamma$. Many systematic uncertainties are canceled in the ratio

TABLE I. Magnitude and phase of intermediate components, and their fit fraction from Dalitz-plot fit of $D^0 \rightarrow K^- \pi^+ \eta$. The quoted uncertainties on the fit fractions are statistical, systematic, and the uncertainty due to the Dalitz model, respectively.

Component	Magnitude	Phase ($^\circ$)	Fit fraction (%)
$\bar{K}^*(892)^0$	1	0	$47.61 \pm 1.32^{+0.24+3.64}_{-0.49-2.71}$
$a_0(980)^+$	2.779 ± 0.032	310.3 ± 1.1	$39.28 \pm 1.50^{+1.58+4.38}_{-0.51-3.30}$
$K\pi$ S-wave	10.82 ± 0.23	50.0 ± 5.7	$31.92 \pm 1.21^{+1.47+2.75}_{-0.53-2.87}$
$K\eta$ S-wave	1.70 ± 0.082	113.8 ± 13.6	$3.37 \pm 0.50^{+0.77+3.20}_{-0.27-1.21}$
$a_2(1320)^+$	1.27 ± 0.079	283.4 ± 4.7	$0.74 \pm 0.09^{+0.06+0.37}_{-0.04-0.17}$
$\bar{K}^*(1410)^0$	4.84 ± 0.36	352.7 ± 2.8	$6.94 \pm 0.85^{+0.55+2.37}_{-1.61-3.22}$
$K^*(1680)^-$	2.56 ± 0.18	232.2 ± 6.6	$1.07 \pm 0.16^{+0.11+0.58}_{-0.10-0.36}$
$K_2^*(1980)^-$	9.29 ± 0.69	207.7 ± 4.0	$1.13 \pm 0.15^{+0.05+0.88}_{-0.05-0.98}$
Sum			$132.1 \pm 3.4^{+1.6+8.3}_{-0.7-4.5}$

measurement, and the dominant uncertainty is that of the η reconstruction efficiency (4%).

IV. DALITZ ANALYSIS

The isobar model [24] is applied for the amplitude of $D^0 \rightarrow (R \rightarrow AB)C$ through a resonance R with spin- J (A , B and C are pseudoscalar particles). The decay amplitude is given by a coherent sum of individual contributions, consisting of a constant term $a_{NR}e^{i\phi_{NR}}$ for the nonresonant three-body decay, and different quasi-two-body resonant decays:

$$\mathcal{M} = a_{NR}e^{i\phi_{NR}} + \sum_R a_R e^{i\phi_R} \mathcal{M}_R(m_{AB}^2, m_{BC}^2). \quad (3)$$

Here m_{AB}^2 and m_{BC}^2 are Dalitz variables, and $a_R e^{i\phi_R}$ is a complex amplitude for the contribution of an individual intermediate resonance R . The amplitude and phase of $\bar{K}^*(892)^0$, having the largest fit fraction, are fixed to $a_{\bar{K}^*(892)^0} = 1$ and $\phi_{\bar{K}^*(892)^0} = 0$. The matrix element \mathcal{M}_R for an intermediate resonant decay is given by

$$\mathcal{M}(ABC|R) = F_D \times F_R \times T_R \times \Omega_J, \quad (4)$$

where $T_R \times \Omega_J$ is a resonance propagator. T_R is a dynamical function for a resonance, described by a relativistic Breit-Wigner (RBW) with mass-dependent width,

$$T_R = \frac{1}{M_R^2 - m_{AB}^2 - iM_R \Gamma_{AB}}, \quad (5)$$

$$\Gamma_{AB} = \Gamma_0^R \left(\frac{p_{AB}}{p_R} \right)^{2J+1} \left(\frac{M_R}{m_{AB}} \right) F_R^2,$$

where p_{AB} (p_R) is the momentum of either daughter in the AB (or R) rest frame, and M_R and Γ_0^R are the nominal mass and width, Ω_J describes the angular momentum that

depends on the spin J by using the Zemach tensor [25,26], and F_D and F_R are Blatt-Weisskopf centrifugal barrier factors [27,28], describing the quark structure of the D^0 meson and intermediate resonance. The parameter of meson radius, R , is set to $5.0 (\text{GeV}/c)^{-1}$ and $1.5 (\text{GeV}/c)^{-1}$ for the D^0 meson and the intermediate resonances, respectively [26]. For the $a_0(980)$ contribution description, we use the Flatté formalism with three coupled channels, $\pi\eta$, $\bar{K}^0 K$ and $\pi\eta'$ [10]

$$T_R(s) = \frac{1}{m_{a_0}^2 - s - i(g_{\pi\eta}^2 \rho_{\pi\eta} + g_{\bar{K}^0 K}^2 \rho_{\bar{K}^0 K} + g_{\pi\eta'}^2 \rho_{\pi\eta'})}, \quad (6)$$

where \sqrt{s} is the invariant mass of $\pi\eta$; g_i and ρ_i are coupling constants and phase-space factors, respectively. For example $\rho_{\pi\eta} = \sqrt{[1 - (m_\pi + m_\eta)^2 / M_{\pi\eta}^2][1 - (m_\pi - m_\eta)^2 / M_{\pi\eta}^2]}$.

The generalized LASS model [29,30] is used to parametrize the $K\pi$ and $K\eta$ S-wave contributions:

$$\mathcal{A}_{g\text{LASS}}(s) = \frac{\sqrt{s}}{2q} \cdot [B \sin(\delta_B + \phi_B) e^{i(\delta_B + \phi_B)} + \sin(\delta_R) e^{i(\delta_R + \phi_R)} e^{2i(\delta_B + \phi_B)}], \quad (7)$$

where s is the invariant mass squared of the $K\pi$ or $K\eta$ system, q is the momentum of K in the $K\pi$ or $K\eta$ rest frame, and δ_B and δ_R are phase angles of the nonresonant component and $K_0^*(1430)$ component, respectively. They are defined as $\tan(\delta_R) = M_r \Gamma(m_{ab}) / (M_r^2 - m_{ab}^2)$ and $\cot(\delta_B) = 1/(aq) + rq/2$, where a , r , B , ϕ_B and ϕ_R are real parameters and may be determined by amplitude analysis.

The DP fit is performed by an unbinned maximum likelihood method with

$$\ln \mathcal{L} = \sum_{i=1}^n \ln[f_s^i(M_i, Q_i) \cdot P_s(m_{K\pi,i}^2, m_{\pi\eta,i}^2) + (1 - f_s^i(M_i, Q_i)) \cdot P_b(m_{K\pi,i}^2, m_{\pi\eta,i}^2)], \quad (8)$$

where n is the number of D^0 candidates in the M and Q 2D signal region and f_s^i is the event-by-event fraction of signal obtained from the M - Q fit; the combinatorial background function, P_b , is a smoothed PDF [23], determined from the DP in the M sideband region ($1.755 \text{ GeV}/c^2 < M < 1.775 \text{ GeV}/c^2$ or $1.935 \text{ GeV}/c^2 < M < 1.955 \text{ GeV}/c^2$) and the Q signal region ($5.35 \text{ MeV}/c^2 < Q < 6.35 \text{ MeV}/c^2$). The signal PDF, P_s , is calculated taking the reconstruction-efficiency dependence on the Dalitz-plot variables into account, and normalized in the Dalitz plot region.

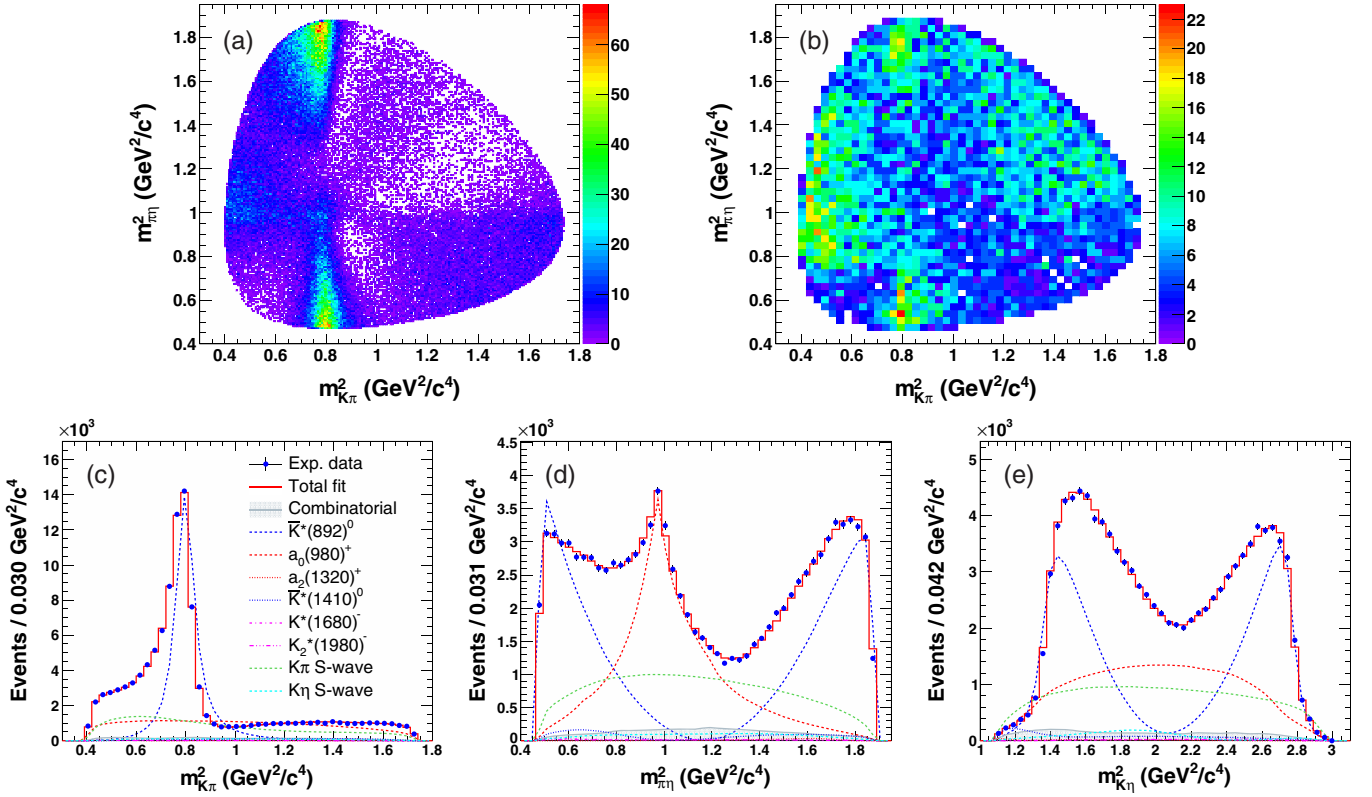


FIG. 2. The Dalitz plot of $D^0 \rightarrow K^- \pi^+ \eta$ in (a) M - Q signal region and (b) M sideband region, and projections on (c) $m_{K\pi}^2$, (d) $m_{\pi\eta}^2$ and (e) $m_{K\eta}^2$. In projections the fitted contributions of individual components are shown, along with contribution of combinatorial background (grey-filled) from sideband region.

$$P_s = |\mathcal{M}(m_{K\pi}^2, m_{\pi\eta}^2)|^2 \epsilon(m_{K\pi}^2, m_{\pi\eta}^2) \int \int dm_{K\pi}^2 dm_{\pi\eta}^2 |\mathcal{M}(m_{K\pi}^2, m_{\pi\eta}^2)|^2 \epsilon(m_{K\pi}^2, m_{\pi\eta}^2). \quad (9)$$

This efficiency distribution $\epsilon(m_{K\pi}^2, m_{\pi\eta}^2)$ is obtained from a high-statistic signal-MC sample and takes into account the known difference in particle identification efficiency for charged tracks between MC and data. These correction factors depend on the momentum and polar angle of individual charged track. The fit fractions (FF) of each intermediate component are calculated across the DP region as

$$FF = \frac{\iint_{DP} |a_R e^{i\phi_R} \mathcal{M}_R(m_{K\pi}^2, m_{\pi\eta}^2)|^2 dm_{K\pi}^2 dm_{\pi\eta}^2}{\iint_{DP} |\mathcal{M}(m_{K\pi}^2, m_{\pi\eta}^2)|^2 dm_{K\pi}^2 dm_{\pi\eta}^2}. \quad (10)$$

The FF uncertainties are evaluated using a Toy MC method in which the sampling takes into account the considerations among all the fitted parameters by propagating the full covariance matrix obtained by the DP fit.

Fifteen possible intermediate resonances [31] were initially considered in the Dalitz analysis. We found $\bar{K}^*(1410)^0$ and $\bar{K}^*(1680)^0$ have a phase-angle difference

of approximately 180° and similar behavior in the DP, therefore, it is hard to separate them. In order to ensure stability of the fit to the Dalitz plot, only $\bar{K}^*(1410)^0$ is kept, while a possible $\bar{K}^*(1680)^0$ contribution is considered as a source of systematic uncertainty. Therefore for the rest of this paper, $K^*(1410)^0$ represents the contribution of $K^*(1410)^0$, $K^*(1680)^0$ and their possible interference. Then, the resonances not contributing to the amplitude significantly are eliminated one by one based on significance-level testing. Significances of individual contributions are determined as the likelihood difference, $\Delta(-2 \ln \mathcal{L})$, that arises when an individual contribution is removed from the model taking into account the degrees of freedom (d.o.f). Only components with significances in excess of 5σ , i.e., $\Delta(-2 \ln \mathcal{L}) > 28.74$ with $\Delta(\text{d.o.f}) = 2$, are retained in the Dalitz model. Of the resonances which were eliminated, $K_2^*(1430)^-$ had the largest significance (3.8σ). A model with eight components is chosen as our nominal model, and this is presented in Fig. 2. It includes six resonances [$a_0(980)^+$, $a_2(1320)^+$, $\bar{K}^*(892)^0$, $\bar{K}^*(1410)^0$, $K^*(1680)^-$, $K_2^*(1980)^-$] and two S-wave components ($K\pi$ and $K\eta$). The fit quality of this nominal model is $\chi^2/\text{d.o.f} = 1638/(1415 - 24) = 1.18$ across the Dalitz plane, and the three Dalitz plot projections are shown in Fig. 2(b-d). The statistical significance of each component is larger than 10σ .

TABLE II. Fitted parameters of the LASS model (with statistical uncertainties only) and their correlation coefficient matrix for $K\pi$ and $K\eta$ S-wave components.

Parameters	Fitted values	Correlation coefficient									
		$B^{K\pi}$	$\phi_B^{K\pi}$	$\phi_R^{K\pi}$	$a^{K\pi}$	$r^{K\pi}$	$B^{K\eta}$	$\phi_B^{K\eta}$	$\phi_R^{K\eta}$	$a^{K\eta}$	$r^{K\eta}$
$B^{K\pi}$	0.239 ± 0.010	1									
$\phi_B^{K\pi}$ (°)	-2.1 ± 0.8	0.094	1								
$\phi_R^{K\pi}$ (°)	-0.7 ± 1.8	0.134	0.738	1							
$a^{K\pi}$ (GeV ^{-1}c)	5.36 ± 0.29	0.172	0.784	0.754	1						
$r^{K\pi}$ (GeV ^{-1}c)	-3.30 ± 0.10	-0.385	0.484	0.409	0.452	1					
$B^{K\eta}$	0.693 ± 0.108	-0.021	0.309	0.351	0.278	-0.185	1				
$\phi_B^{K\eta}$ (°)	1.3 ± 3.4	-0.318	0.387	0.340	0.432	0.529	-0.338	1			
$\phi_R^{K\eta}$ (°)	25.5 ± 9.1	-0.210	-0.746	-0.756	-0.804	-0.250	-0.199	-0.447	1		
$a^{K\eta}$ (GeV ^{-1}c)	0.293 ± 0.048	-0.373	-0.711	-0.696	-0.790	-0.214	-0.173	-0.509	0.784	1	
$r^{K\eta}$ (GeV ^{-1}c)	-15.9 ± 2.6	-0.381	-0.694	-0.675	-0.776	-0.218	-0.092	-0.528	0.774	0.995	1

In particular, the statistical significance of the $K\eta$ S-wave component with $K_0^*(1430)^-$ is greater than 30σ , and $K^*(1680)^- \rightarrow K^-\eta$ and $K_2^*(1980)^- \rightarrow K^-\eta$ are observed for the first time and have statistical significances of 16σ and 17σ , respectively. The fitted magnitudes and phases of intermediate components are listed in Table I, together with corresponding fit fractions, where statistical uncertainties are obtained from 500 sets of toy MC samples, and systematic uncertainties take into account model uncertainties and other systematic uncertainties as discussed in Sec. V. The fact that the sum of fit fractions is greater than 100% indicates significant destructive interference. Table II shows the fitted parameters of LASS model in Eq. (7) and their correlation coefficient matrix for the $K\pi$ and $K\eta$ S-wave components. The left coefficients in the full correlation matrix from Dalitz fit are shown in Table III including the correlation coefficients among the magnitudes and phases of resonances and the LASS model parameters. Various Dalitz models, including the nominal model used in the fit to final experimental data, are produced using MC to perform tests for any possible bias, and to check that the input and output Dalitz parameters are consistent. We also checked for the existence of possible multiple solutions in the fit, with likelihood scanning of each of the free parameters. In addition, 100 sets of Dalitz fits were performed by sampling the initial values of free parameters uniformly in an interval around their final values. No multiple solutions were found.

To investigate the parameters of the Flatté formulation of the $a_0(980)^+$ line shape, the Dalitz fit based on the nominal model with free $g_{\pi^\pm\eta}$ is also performed and this yields $g_{\pi^\pm\eta} = 0.596 \pm 0.008(\text{stat}) \text{ GeV}/c^2$. This value is consistent with the measurement of BESIII, $0.607 \pm 0.011 \text{ GeV}/c^2$ [10]. The significance of the $\pi\eta'$ contribution is tested and the results with floated $g_{\pi\eta'}$ and fixed $g_{\pi\eta'} = 0$ give $\Delta(-2\ln L) = 102$ with $\Delta(\text{d.o.f}) = 1$, which indicates a $\pi\eta'$ contribution with 10.1σ statistical

significance. The fitted $g_{\pi\eta'} = 0.408 \pm 0.018(\text{stat}) \text{ GeV}/c^2$ is also consistent with the BESIII measurement of $g_{\pi\eta'} = 0.424 \pm 0.050 \text{ GeV}/c^2$ [10].

V. SYSTEMATIC UNCERTAINTIES

The systematic uncertainties are divided into the uncertainties arising from the Dalitz model used in the fit and those from other sources. The model systematic uncertainties arise from the choice of individual components in the model, and from the parametrization of intermediate structures. The effective barrier radial parameter, R , is varied between 0 and $3.5 (\text{GeV}/c)^{-1}$ for intermediate resonances, where the maximum value is chosen as the measured R value for the narrowest resonance, the $K^*(892)$ ($R = 3.0 \pm 0.5 (\text{GeV}/c)^{-1}$ [6]), increased by its statistical error. Three coupling factors of the Flatté function are varied within the quoted uncertainties, and the largest difference with respect to the nominal model is assigned as the systematic uncertainty due to this source. The masses and widths of intermediate resonances are varied within their uncertainties [6]. To account for the $K\pi$ and $K\eta$ S-wave components, the model used in the fit is modified by adding a wide resonance κ described by a complex pole function [32] for a $K\pi$ S-wave, and $K_0^*(1950)^-$ described by RBW for a $K\eta$ S-wave. The nonsignificant resonance $a_0(1450)^+$ is added to evaluate the $\pi\eta$ S-wave component uncertainty. We also use a $\bar{K}^*(1680)^0$ resonance instead of a $\bar{K}^*(1410)^0$ contribution.

The systematic uncertainty due to the Dalitz distribution of combinatorial background is evaluated by (1) varying the M sideband region within a shift of $\pm 5 \text{ MeV}/c^2$, and by (2) correcting the Dalitz distribution of experimental data in the M sideband by the ratio of combinatorial background in the M signal and sideband regions from generic MC. The larger difference is assigned as the

TABLE III. The correlation coefficients among the resonant parameters: the magnitudes (mag.) and phases, and the LASS model parameters for $K\pi$ and $K\eta$ S-wave components from Dalitz fit.

Parameters	$a_0(980)^+$		$a_2(1320)^+$		$\bar{K}^*(1410)^0$		$K^*(1680)^-$		$K_2^*(1980)^-$		$(K\pi)_{S\text{-wave}}$		$(K\eta)_{S\text{-wave}}$	
	Magnitudes	Phase	Magnitudes	Phase	Magnitudes	Phase	Magnitudes	Phase	Magnitudes	Phase	Magnitudes	Phase	Magnitudes	Phase
$a_0(980)^+$	1													
$a_2(1320)^+$	Magnitudes	1												
	Phase	-0.011												
$\bar{K}^*(1410)^0$	Magnitudes	-0.250	0.188	1										
	Phase	-0.378	-0.143	-0.114	1									
$K^*(1680)^-$	Magnitudes	-0.699	0.130	-0.024	0.511	1								
	Phase	0.555	-0.513	-0.196	-0.406	-0.666	1							
$K_2^*(1980)^-$	Magnitudes	-0.516	0.244	0.231	0.194	0.596	-0.240	1						
	Phase	0.455	-0.495	-0.045	-0.237	-0.827	0.707	-0.572	1					
$(K\pi)_{S\text{-wave}}$	Magnitudes	0.080	-0.585	0.092	0.097	-0.345	0.469	-0.302	0.566	1				
	Phase	0.208	-0.606	-0.514	-0.164	-0.232	0.62	-0.237	0.441	0.350	1			
$(K\eta)_{S\text{-wave}}$	Magnitudes	0.330	-0.218	0.095	-0.483	-0.582	0.655	-0.327	0.502	0.546	0.246	1		
	Phase	-0.222	0.649	0.066	0.143	0.571	-0.65	0.521	-0.812	-0.652	-0.461	-0.609	1	
LASS of $K\pi$	Magnitudes	0.493	-0.503	-0.189	-0.326	-0.687	0.765	-0.472	0.804	0.501	0.528	0.587	-0.839	1
	Phase	0.375	-0.451	-0.194	-0.089	-0.615	0.515	-0.615	0.790	0.419	0.376	0.315	-0.853	0.768
S-wave	B	0.051	-0.383	-0.137	0.170	-0.157	0.026	-0.350	0.371	0.117	0.345	-0.375	-0.199	0.171
	ϕ_B	0.210	-0.538	0.014	-0.186	-0.544	0.607	-0.438	0.729	0.654	0.401	0.611	-0.858	0.731
S-wave	ϕ_R	0.149	-0.475	-0.011	-0.207	-0.486	0.561	-0.373	0.644	0.550	0.377	0.689	-0.842	0.738
	a	0.302	-0.653	0.022	-0.187	-0.622	0.677	-0.534	0.812	0.702	0.482	0.637	-0.934	0.739
LASS of $K\eta$	r	0.335	-0.176	0.159	-0.258	-0.425	0.422	-0.184	0.301	0.461	0.086	0.678	-0.285	0.255
	B	-0.064	-0.290	-0.201	0.268	0.112	0.065	-0.026	0.156	0.152	0.125	-0.012	-0.443	0.440
S-wave	ϕ_B	0.325	-0.179	0.163	-0.599	-0.566	0.686	-0.106	0.405	0.286	0.257	0.729	-0.345	0.369
	ϕ_R	-0.454	0.441	0.129	0.329	0.716	-0.713	0.560	-0.784	-0.451	-0.414	-0.584	0.872	-0.786
S-wave	a	-0.351	0.528	0.040	0.258	0.712	-0.694	0.524	-0.845	-0.516	-0.443	-0.523	0.830	-0.736
	r	-0.329	0.517	0.024	0.262	0.702	-0.681	0.519	-0.830	-0.512	-0.435	-0.520	0.807	-0.692
														-0.752

TABLE IV. Sources of systematic uncertainties for each amplitude. For model systematic uncertainty: (1) Effective barrier radius R ; (2) Flatté coupling parameters g_i ; (3) masses of resonances; (4) widths of resonances; (5) $K\pi$ S-wave uncertainty; (6) $K\eta$ S-wave uncertainty; (7) $\pi\eta$ S-wave uncertainty; (8) $\bar{K}^*(1680)^0$ instead of $\bar{K}^*(1410)^0$. For other sources: (9) signal fraction; (10) signal region; (11) background distribution; (12) efficiency variations; (13) best candidate selection for multicandidates.

Sources		$\bar{K}^*(892)^0$	$a_0(980)^+$	$K\pi$ S-wave	$K\eta$ S-wave	$a_2(1320)^+$	$\bar{K}^*(1410)^0$	$K^*(1680)^-$	$K_2^*(1980)^-$	$\sum FF$
Model systematic (%)	1)	+3.63 -2.64	+3.26 -1.89	+1.89 -1.34	+0.28 -0.00	+0.25 -0.10	+1.37 -1.53	+0.48 -0.01	+0.85 -0.94	+7.27 -3.47
	2)	+0.10 -0.09	+2.11 -2.13	+0.90 -1.01	+0.22 -0.20	+0.05 -0.05	+0.83 -0.68	+0.16 -0.13	+0.14 -0.09	+2.44 -2.40
	3)	+0.17 -0.18	+1.65 -1.64	+0.80 -2.10	+2.42 -1.01	+0.02 -0.02	+1.14 -1.81	+0.16 -0.20	+0.08 -0.11	+1.50 -1.53
	4)	+0.15 -0.39	+0.69 -0.26	+1.04 -0.96	+1.43 -0.51	+0.26 -0.12	+1.30 -1.98	+0.15 -0.08	+0.13 -0.08	+0.76 -0.48
	5)	+0.15	+0.62	+1.01	+1.47	+0.03	-0.57	-0.23	-0.07	+2.41
	6)	+0.06	-0.06	+0.65	-0.29	+0.00	-0.19	-0.13	+0.02	+1.07
	7)	-0.09	-0.20	-0.33	+0.15	+0.00	+0.23	+0.00	+0.07	-0.16
	8)	-0.43	+0.74	-0.05	-0.22	+0.03	+0.16	+0.17	-0.23	+0.17
	Total	+3.64 -2.71	+4.38 -3.30	+2.75 -2.87	+3.20 -1.21	+0.37 -0.17	+2.37 -3.22	+0.58 -0.36	+0.88 -0.98	+8.28 -4.52
	9)	+0.03 -0.06	+0.05 -0.06	+0.15 -0.00	+0.06 -0.00	+0.01 -0.00	+0.05 -0.06	+0.01 -0.00	+0.01 -0.00	+0.14 -0.01
Other systematic (%)	10)	+0.10 -0.19	+0.00 -0.46	+0.80 -0.50	+0.21 -0.22	+0.05 -0.03	+0.33 -0.15	+0.06 -0.10	+0.04 -0.02	+0.54 -0.65
	11)	+0.06 -0.22	+0.54 -0.22	+0.35 -0.16	+0.14 -0.16	+0.03 -0.01	+0.44 -0.22	+0.07 -0.02	+0.03 -0.05	+0.62 -0.20
	12)	+0.21 -0.00	+0.04 -0.04	+0.16 -0.04	+0.14 -0.00	+0.01 -0.00	+0.00 -0.21	+0.05 -0.00	+0.01 -0.00	+0.22 -0.05
	13)	-0.39	+1.48	+1.16	+0.71	-0.02	-1.57	+0.01	+0.00	+1.29
	Total	+0.24 -0.49	+1.58 -0.51	+1.47 -0.53	+0.77 -0.27	+0.06 -0.04	+0.55 -1.61	+0.11 -0.10	+0.05 -0.05	+1.55 -0.68

systematic uncertainty due to the background distribution. The systematic uncertainty related to efficiency is estimated in two ways: (1) removing the correction for PID efficiency, and (2) shifting the $p^*(D^*)$ limit by ± 0.05 GeV/ c to consider possible discrepancy between MC and experimental data in $p^*(D^*)$ spectrum. These uncertainties are combined quadratically to give a systematic uncertainty due to efficiency. Comparing with the nominal fit model, the difference in the fit results when the signal fraction is varied by $\pm 1\sigma$ (as determined from the M - Q fit) is taken as the systematic uncertainty due to the uncertainty in the fraction of signal in the sample. A shift of the signal region by ± 5 MeV/ c^2 in M or ± 0.1 MeV/ c^2 in Q is applied to estimate the effect of the signal region selection. The larger difference in fit fraction is kept as the uncertainty due to this source. The uncertainty of multi-candidate selection is estimated by randomly selecting one of the multicandidates as the best candidate instead of our nominal BCS method. The sources of systematic uncertainty considered are summarized in Table IV. Individual uncertainties are added in quadrature.

VI. FURTHER STUDY AND DISCUSSION

In this section, we present further discussion of the Dalitz fit results shown in Table I and of our measured branching fraction $\mathcal{B}(D^0 \rightarrow K^- \pi^+ \eta) = (1.973 \pm 0.009(\text{stat}) \pm 0.079(\text{syst}) \pm 0.018(\mathcal{B}_{\text{PDG}}))\%$.

- (i) $D^0 \rightarrow \bar{K}^*(892)^0 \eta$ decay: we determine $\mathcal{B}(D^0 \rightarrow [\bar{K}^*(892)^0 \rightarrow K^- \pi^+] \eta) = (0.94 \pm 0.03(\text{stat})_{-0.07}^{+0.08}(\text{syst}) \pm 0.01(\mathcal{B}))\%$. Using $\mathcal{B}(\bar{K}^*(892)^0 \rightarrow K^- \pi^+) = (66.503 \pm 0.014)\%$ [6], we find $\mathcal{B}(D^0 \rightarrow \bar{K}^*(892)\eta) = (1.41 \pm 0.04(\text{stat})_{-0.11}^{+0.12}(\text{syst}) \pm 0.01(\mathcal{B}_{\text{PDG}}))\% = (1.41_{-0.12}^{+0.13})\%$, which is consistent with, and more precise than, the current world average $(1.02 \pm 0.30)\%$ [6]. It deviates from the theoretical predictions of $(0.51\text{--}0.92)\%$ [1–3] with a significance of more than 3σ .
- (ii) $K^*(1680) \rightarrow K\eta$ decay: we determine $\mathcal{B}(D^0 \rightarrow [K^*(1680)^- \rightarrow K^- \eta] \pi^+) = (2.11 \pm 0.32(\text{stat})_{-0.72}^{+1.16}(\text{syst}) \pm 0.02(\mathcal{B})) \times 10^{-4}$. Using $\mathcal{B}(D^0 \rightarrow [K^*(1680)^- \rightarrow K^- \pi^0] \pi^+) = (0.19 \pm 0.07)\%$ [6] and $\mathcal{B}(K^*(1680)^- \rightarrow K^- \pi^0) = (12.90 \pm 0.83)\%$ [6], the branching fraction of $D^0 \rightarrow K^*(1680)^- \pi^+$ is $(1.47 \pm 0.55)\%$. Thus, one obtains $\mathcal{B}(K^*(1680)^- \rightarrow K^- \eta) = (1.44 \pm 0.21(\text{stat})_{-0.49}^{+0.79}(\text{syst}) \pm 0.54(\mathcal{B}_{\text{PDG}}))\%$, where the uncertainties are respectively statistical, systematic, and due to the branching fraction uncertainties in Ref. [6]. Finally, the relative branching ratio of $K^*(1680)^-$ to $K^- \eta$ and $K^- \pi^0$ [6] is measured to be $0.11 \pm 0.02(\text{stat})_{-0.04}^{+0.06}(\text{syst}) \pm 0.04(\mathcal{B}_{\text{PDG}})$, which is not consistent with theoretical predictions (≈ 1.0) under the assumption that $K^*(1680)$ is a pure 1^3D_1 state [8,9]. This ratio is comparable to $\mathcal{B}(K_0^*(1430) \rightarrow K\eta)/\mathcal{B}(K_0^*(1430) \rightarrow K\pi) = 0.09_{-0.04}^{+0.03}$.

[6], which is consistent with the theoretical prediction assuming that $K^*(1430)$ is a 1^3P_0 state [8,9].

- (iii) $K_2^*(1980) \rightarrow K\eta$ decay: we measure for the first time $\mathcal{B}(D^0 \rightarrow [K_2^*(1980)^- \rightarrow K^- \eta] \pi^+) = (2.2 \pm 0.2(\text{stat})_{-1.9}^{+1.7}(\text{syst}) \pm 0.0(\mathcal{B}_{\text{PDG}})) \times 10^{-4} = (2.2_{-1.9}^{+1.7}) \times 10^{-4}$, which is strongly suppressed due to a limit of the phase-space region and yet allowed due to a large width of $K_2^*(1980)$.

VII. CONCLUSION

In summary, using 953 fb^{-1} of data collected by the Belle detector, a Dalitz plot analysis of $D^0 \rightarrow K^- \pi^+ \eta$ is performed. The DP is well represented by a combination of significant quasi-two-body decay channels with six intermediate resonances: $\bar{K}^*(892)^0$, $a_0(980)^+$, $a_2(1320)^+$, $\bar{K}^*(1410)^0$, $K^*(1680)^-$, $K_2^*(1980)^-$, and two S-wave components of $K\pi$ and $K\eta$. The fit fraction of each component is given in Table I. The dominant contributions to the decay amplitude arise from $\bar{K}^*(892)^0$, $a_0(980)^+$ and the $K\pi$ S-wave component. The $K\eta$ S-wave component, including $K_0^*(1430)^-$, is observed with a statistical significance of more than 30σ , and the decays $K^*(1680)^- \rightarrow K^- \eta$ and $K_2^*(1980)^- \rightarrow K^- \eta$ are observed for the first time and have statistical significances of 16σ and 17σ , respectively.

We measure the ratio of the branching fractions, $\frac{\mathcal{B}(D^0 \rightarrow K^- \pi^+ \eta)}{\mathcal{B}(D^0 \rightarrow K^- \pi^+)} = 0.500 \pm 0.002(\text{stat}) \pm 0.020(\text{syst}) \pm 0.003(\mathcal{B}_{\text{PDG}})$ for the first time. The relative branching ratio $\frac{\mathcal{B}(K^*(1680)^- \rightarrow K^- \eta)}{\mathcal{B}(K^*(1680)^- \rightarrow K^- \pi^0)}$ is determined to be $0.11 \pm 0.02(\text{stat})_{-0.04}^{+0.06}(\text{syst}) \pm 0.04(\mathcal{B}_{\text{PDG}})$. This is not consistent with the theoretical prediction under an assumption of a pure 1^3D_1 state [8,9]. We also determine the product of branching fraction $\mathcal{B}(D^0 \rightarrow [K_2^*(1980)^- \rightarrow K^- \eta] \pi^+) = (2.2_{-1.9}^{+1.7}) \times 10^{-4}$. For $a_0(980)^+$, we confirm the $\pi\eta'$ contribution in the three-channel Flatté model with a statistical significance of 10.1σ . We have also determined the branching fraction $\mathcal{B}(D^0 \rightarrow \bar{K}^*(892)^0 \eta) = (1.41_{-0.12}^{+0.13})\%$, which is consistent with, and more precise than, the current world average of $(1.02 \pm 0.30)\%$ [6]. It deviates from the various theoretical predictions of $(0.51\text{--}0.92)\%$ [1–3] with a significance of more than 3σ .

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